# The SAS LGTPHCURV9 Macro 

Ruifeng Li, Ellen Hertzmark, Mary Louie, Linlin Chen, and Donna Spiegelman

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#### Abstract

The \%LGTPHCURV9 macro fits restricted cubic splines to unconditional logistic, pooled logistic, conditional logistic, and proportional hazards regression models to examine non-parametrically the (possibly non-linear) relation between an exposure and the odds ratio (OR) or incidence rate ratio (IRR) of the outcome of interest. It allows for controlling for covariates. It also allows stepwise selection among spline variables. The output is the set of p -values from the likelihood ratio tests for non-linearity, a linear relation, and any relation, as well as a graph of the OR, IRR, predicted cumulative incidence or prevalence, or the predicted incidence rate (IR), with or without its confidence band. The confidence band can be shown as the bounds of the confidence band, or as a "cloud" (gray area) around the OR/IRR/RR curve. In addition, the macro can display a smoothed histogram of the distribution of the exposure variable in the data being used.

Keywords: SAS version 9.1, macro, logistic regression, proportional hazards regression, Cox regression, cubic splines, nonlinearity, curves, smoothed histogram, plotting, stepwise selection, incidence rate, odds ratio, rate ratio


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## 1 Description

\%LGTPHCURV9 is a SAS macro that examines the relationship between a continuous exposure (EXPOSURE) and a dichotomous outcome (CASE) or failure time (TIME), controlling for covariates. It also produces publication-quality graphs of this relationship.

## 2 Invocation and Details

In order to run this macro, your program must know where to look for it. You can tell SAS where to look for macros by using the options

```
options nocenter ps=78 ls=80 replace formdlim='='
mautosource
sasautos=('/usr/local/channing/sasautos',
    '/proj/nhsass/nhsas00/nhstools/sasautos');
```

This will allow you to use all the SAS read macros for the data sets in /proj/nhsass/nhsas00/nhstools/sasautos as well as other public SAS macros, such as \%PM, \%INDIC3, \%EXCLUDE, \%MPHREG, \%CALADJ, and \%PCTL in /usr/local/channing/sasautos.

In the rest of this section, we will list all the input parameters, some of which are required and some of which are optional, but strongly suggested, and some of which are truly optional.

NOTE: if a parameter has a default value, it is given to the right of the ' $=$ '.

```
REQUIRED PARAMETERS
====================
    DATA = < the name of the input dataset,
    EXPOSURE = < variable name of the exposure of interest,
    CASE = < variable name of the outcome (LOGISTIC) or
        censoring variable (CONDLOG or COX),
        coded O (non-case or censored) or 1 (case or not censored) >,
    TIME = < censored failure time for COX or conditional logistic models >,
        NOTE: if this parameter is not null (blank), LGTPHCURV9 will
                        automatically fit a COX model.
```

STRONGLY SUGGESTED PARAMETERS
==============================
OUTPLOT = PS < type of software in which to make the plot:
PS=encapsulated postscript (the default),
other options are JPEG and HTML >,
PICTNAME $=$ < filename of the file for the plot.
You should give a mnemonic name for this >.
default= <name of dataset>.<exposure>.<outplot>
If you are experimenting with number of knots, or with
linear vs. spline plots, or with axis specifications,
and do not give a value for PICTNAME,
you will end up with only the most recently made graph with
the given EXPOSURE variable >,
REFVAL $=$ MIN < the reference value for the exposure variable, options are data-derived MEAN, MIN, MEDIAN, MODE, or a value you supply >,
AXORDV $=$ < range of the vertical axis and tick-mark spacing for odds ratio or rate ratio plots, (<low> to <high> by <increment>) >,
AXORDI $=$ < range of the vertical axis and tick mark spacing for incidence rate plots, (<low> to <high> by <increment>) >,
AXORDP $=$ < range of the vertical axis and tick mark spacing for predicted probability plots, (<low> to <high> by <increment>) >,
HLABEL $=<$ label for the horizontal axis >,
VLABEL $=<$ label for the vertical axis, for odds ratio or rate ratio plots >,
VLABELI $=<$ label for the vertical axis, for incidence rate plots >,
VLABELP $=<$ label for the vertical axis, for predicted probability plots >,

PARAMETERS RELATED TO THE INPUT DATA SET

| LPCT | $=$ < to delete from the data set used to fit the spline model observations with EXPOSURE below a percentile you specify >, |
| :---: | :---: |
| HPCT | $=<$ to delete from the data set used to fit the spline model observations with EXPOSURE above a percentile you specify >, |
| LOWCUT | $=$ < to delete from the data set used to fit the spline model observations with EXPOSURE below a value that you specify >, |
| HICUT | $=$ < to delete from the data set used to fit the spline model observations with EXPOSURE above a value that you specify >, |
| WHERE | $=<\mathrm{a}$ sub-setting clause to restrict the data used > , |
| EXTRAV | $=$ < extra variables to be kept in the working data set, primarily for use in the WHERE parameter. for example if the WHERE parameter refers to a variable not in the EXPOSURE, ADJ, CASE, BYVAR, or TIME, you MUST list this variable here >, |

PARAMETERS RELATED TO THE MODEL

| $=============================$ |  |
| ---: | :--- |
| MODEL $=$ | LOGISTIC < the type of model you want to run |
|  | $\quad$ (LOGISTIC, CONDLOG, or COX) >, |
| ADJ $=$ | < the list of covariates >, |
| STRATA $=$ | < matching strata for COX or CONDLOG model |
|  | $\quad$ (typically used for conditional logistic regression) >, |
| NK $=$ | < number of automatically placed knots to use >, |

```
The only values of NK currently supported are \(3,4,5,6,7,8,9,10,17,21,25\), and 50. If you do not specify a value for NK or give a list of knot locations in KNOT (see next), the macro will set NK=21 if automatic stepwise selection (SELECT=3) is specified or NK=4 otherwise.
KNOT = < values of EXPOSURE at knot points, if you want to specify the knots yourself >
One situation in which you need to use KNOT= is when the distribution of the data is such that the automatic positioning of the knot points by their percentile values does not yield NK distinct knots. This happens in NHS, with NK=4 for EXPOSURE= alcohol consumption.
MODOPT \(=\) < options to be used in the model statement, e.g. to control the number of iterations or the criteria for convergence >,
SELECT \(=1\) < whether to use all spline variables in model:
1 = use all
2 = use spline variables provided by user (e.g. based on a previous selection procedure)
3 = use automatic stepwise selection >, NOTE: If you use SELECT=3 with automatically placed knots and have not specified NK, the macro sets \(\mathrm{NK}=21\).
SLS \(\quad=.05<p\) value for entry into model, if SELECT=3 >,
SLE \(\quad=.05<p\) value to stay in the model, if SELECT=3 >,
USERSPLV = <list of spline variables to be included if SELECT=2 (does not include the linear variable EXPOSURE)>,
PARAMETERS RELATED TO THE OUTPUT
```

```
=================================
```

=================================
MODPRINT = T < whether to print output generated by PROC
MODPRINT = T < whether to print output generated by PROC
LOGISTIC or PROC PHREG,
LOGISTIC or PROC PHREG,
F = suppress, T = print >,
F = suppress, T = print >,
While some of the examples in this documentation use
While some of the examples in this documentation use
MODPRINT=F, we strongly suggest that users leave
MODPRINT=F, we strongly suggest that users leave
MODPRINT at the default.
MODPRINT at the default.
PRINTCV = F < whether to print the covariances of the
PRINTCV = F < whether to print the covariances of the
coefficients in the .log >,
coefficients in the .log >,
TESTREP = LONG <specify long or short report on test for
TESTREP = LONG <specify long or short report on test for
        non-linearity > (SHORT to be used only if you really
non-linearity > (SHORT to be used only if you really
don't need the wordy directions).
don't need the wordy directions).
HEADER1 = < Description of the analysis to be used in the
HEADER1 = < Description of the analysis to be used in the
report of the test for non-linearity >,
report of the test for non-linearity >,
PRINTPOINTS = < a list of values of EXPOSURE for which you wish
PRINTPOINTS = < a list of values of EXPOSURE for which you wish
the macro to print the numeric values of
the macro to print the numeric values of
what is plotted in the graph >,

```
                what is plotted in the graph >,
```

```
PLOTPRINT = F <whether you want the macro to print the whole set
    of plotting points >,
```

PARAMETERS RELATED TO THE GRAPH OF THE REGRESSION SPLINE

```
PLOT = 2 < type of graphics you want:
    O = NO PLOT (i.e. just do test for non-linearity)
    1 = PROC PLOT (prints in .saslog)
    2 = PROC GPLOT
    3 = PROC PLOT and PROC GPLOT,
    4 = text file for use with PC software or other
                graphing programs >,
PWHICH = SPLINE < whether to plot results of linear or
    spline model (LINEAR or SPLINE) >,
GRAPHTIT = < label (title) for the top of the plot.
    If the value is NONE (upper case required),
    the graph will have no title.
    If GRAPHTIT is empty, HEADER1 will be used. >,
TITLEFONT= swissb < font to use for graph title, if any >,
TITLEMULT= 1 < multiplier to make font of title larger or smaller>,
FOOTER = default < footnote for the bottom of the plot
    DEFAULT lists the first 8 covariates as listed in ADJ.
    The user might prefer to list the conceptual variables
    (e.g. age, time period, BMI).
    To avoid the footnote entirely, use NONE
    (upper case required) >,
FOOTFONT= swiss < font for footnote, if any>,
FOOTMULT= 1 < multiplier to change size of footnote>,
AXLABFONT= swissb < font for axis labels >,
AXLABMULT= 1 < multiplier to change size of axis labels >,
AXVALFONT= swiss < font for axis values >,
AXVALMULT= 1 < multiplier to change size of axis values >,
PLOTORRR = T < whether to plot the confidence band >,
CI = 2 < type of 95% confidence intervals to be displayed
        (1=clouds, 2=dotted lines) >,
E = T < whether to plot the OR/RR or the log(OR/RR),
        E=T is to plot OR/RR,
        E=F is to plot log(OR/RR) >,
AXORDVLOG10 = F < whether to plot the vertical axis on the log10 scale.
                    This is useful if your OR or RR has a wide range
                    (and you really want to show it, as opposed to
                    trimming the data or using CUTOFF (see above) )
                    NOTE: Setting AXORDVLOG10=T will result in a WARNING:
                    The ORDER= list on axis statement 2 was ignored because
                    the log of 0 is undefined >,
VLABELSTYLE = V <whether to have the vertical axis label run parallel
            to the axis (V) or to have it print horizontally (H) >,
ORDATA = < name of the dataset that contains odds
                        ratio/incidence rate ratio
```



PARAMETERS RELATED TO DISPLAY OF EXPOSURE DISTRIBUTION


```
    DISPLAYX = T < whether to display the distribution of the
                        exposure variable (EXPOSURE),
                        F=none,
                        T=smoothed histogram>,
    TECHNICAL PARAMETERS RELATED TO DISPLAY OF EXPOSURE DISTRIBUTION
    WE STRONGLY SUGGEST THAT USERS LEAVE THESE PARAMETERS AT THEIR
    DEFAULT VALUES, unless the procedure does not converge.
    ---------------
    BWM = 1 < smoothing parameter for frequency
            histogram (DISPLAYX=T only) >,
            Larger numbers usually result in more smoothed
            (less detailed) graphs>,
DISTMETH=SJPI < method for making smoothed histogram
                    (DISPLAYX=T only),
                    SJPI=Sheather-Jones plug-in
                    SNR=simple normal reference
                    SROT=Silverman's rule of thumb
                    OS=oversmoothed
                    NOTE: If you get a diagnostic message saying that
                the Sheather-Jones plug-in does not converge, try
                one of the other methods or increase BWM >,
N_GRID = 500 <number of intervals/grids between minimum and
            maximum values of EXPOSURE (SMOOTH option only) >,
MAKING A FILE FOR PC GRAPHICS, PLOT=4 ONLY
===========================================
    PLOTDATA = <&DATA>.<&EXPOSURE>.txt
    < file name of output for PLOT=4 >,
    FILEMODE = MOD < output mode for PLOTDATA file >.
```

For example, if we use option $\{\backslash e m$ PLOT\}=4 for Example 3 below (instead of $\{\backslash e m$ PLOT\}=2), the first 5 lines of the ASCII file will look like:

| BMI | Splan | lower | Upper |
| :--- | :--- | :--- | :--- |
| 16.07 | 2.927 | 1.842 | 4.652 |
| 16.11784 | 2.894 | 1.830 | 4.577 |
| 16.16568 | 2.862 | 1.818 | 4.503 |
| 16.21352 | 2.829 | 1.807 | 4.430 |

Note: The first column is the exposure values; the second column is the estimated values of the linear combination of exposure plus the selected spline variables (If $P L O T O R R R=\mathrm{T}$, they are odds ratios if the model is logistic or rate ratios if $M O D E L=\mathrm{COX}$; if $P L O T P R O B=\mathrm{T}$, they are the predicted probabilities for the average time represented by one observation (e.g. 2 years in most channing studies); if PLOTINC $=T$, they are the predicted probabilities and the incidence rates); the third and fourth are the $95 \%$ lower and upper confidence values of the second column. If you
use option CUTOFF, it is possible to have missing values (if the real values are bigger than the cutoff points).

## 3 Examples

Examples 1-6 and 8-10 use data from a case-control study of ovulatory infertility in NHS II. The exposures of interest are BMI and hours of vigorous exercise per week. Example 7 uses data from a study of smoking and lung cancer among current smokers in NHS. Example 11 uses data from a case-control study of CHD using blood measurements, and Example 12 shows a stratified proportional hazards model.

### 3.1 Example 1. Required parameters not given (to demonstrate ERROR messages)

In the following call to \%LGTPHCURV9, I neglected to give values for EXPOSURE and CASE. In addition, since it calls for a CONDLOG model, the TIME and STRATA parameters are required.

The macro call is:

```
title2 'example 1--errors in macro call';
%lgtphcurv9(data=merge0, model=condlog, refval=22, displayX=T,
pictname=pregc21.bmi4apd, hlabel=%quote(BMI (kg / sq m)));
```

The macro printed out the following diagnostic messages in both the .log and the .lst files, then stopped.

```
/udd/stleh/doctn/lgtphcurv Program example1-6 13JAN2011 22:09
example 1--errors in macro call
ERR'OR in MACRO call: You did not give one or more of the required parameters.
    You did not give a variable name to use as EXPOSURE, as required
    You did not give a variable name to use as CASE, as required
    You did not name a TIME variable,
        as required when you use model=COX or CONDLOG.
    You did not name a STRATA parameter,
        as required when you use model=CONDLOG.
```


### 3.2 Example 2. Bare bones invocation

This analysis uses no optional parameters (except MODPRINT).

The macro call is

```
title2 'example 2--bare bones';
%lgtphcurv9(data=merge0, exposure=BMI, case=case,
    adj= age2 age3 age4 period2 period3);
```

The output is
example 2--bare bones
Percent of range of BMI below the first knot is 11 .
Percent of range of BMI above the last knot is 38 .
example 2--bare bones
Knots for BMI:
18.6421 .1423 .5231 .02
example 2--bare bones
values of spline variables when BMI is 16.07000000
Obs BMI BMI1 BMI2
$\begin{array}{llll}27103 & 16.07 & 0 & 0\end{array}$
example 2--bare bones

Analysis of Maximum Likelihood Estimates \& Odds Ratio (with adjusters only)

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :--- | ---: | ---: | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |
| Intercept | -3.3729 | 0.0659 | $<.0001$ | 0.03429 | 0.03013 | 0.03902 |
| AGE2 | -0.2041 | 0.0813 | 0.0120 | 0.81539 | 0.69532 | 0.95620 |
| AGE3 | -0.2336 | 0.1075 | 0.0297 | 0.79164 | 0.64129 | 0.97724 |
| AGE4 | 0.5820 | 0.1774 | 0.0010 | 1.78963 | 1.26410 | 2.53363 |
| PERIOD2 | 0.1406 | 0.0798 | 0.0782 | 1.15096 | 0.98425 | 1.34591 |
| PERIOD3 | -0.0415 | 0.0988 | 0.6744 | 0.95932 | 0.79036 | 1.16441 |

example 2--bare bones

| Association of Predicted Probabilities and Observed R |  |  |  |
| :--- | :---: | :--- | ---: |
| measure |  |  |  |
|  | value | measure | value |
| Percent Concordant | 42.7 | Somers' D | 0.100 |
| Percent Discordant | 32.7 | Gamma | 0.133 |
| Percent Tied | 24.6 | Tau-a | 0.006 |
| Pairs | 21907512 | c | 0.550 |

example 2--bare bones

Analysis of Maximum Likelihood Estimates \& Odds Ratios (linear model with adjust

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Intercept | -4.6925 | 0.1989 | $<.0001$ | 0.00916 | 0.00621 | 0.01353 |
| AGE2 | -0.2243 | 0.0814 | 0.0059 | 0.79904 | 0.68118 | 0.93729 |
| AGE3 | -0.2798 | 0.1078 | 0.0094 | 0.75592 | 0.61198 | 0.93372 |
| AGE4 | 0.5224 | 0.1779 | 0.0033 | 1.68612 | 1.18987 | 2.38934 |
| PERIOD2 | 0.1280 | 0.0799 | 0.1094 | 1.13654 | 0.97171 | 1.32933 |
| PERIOD3 | -0.0780 | 0.0991 | 0.4311 | 0.92496 | 0.76170 | 1.12322 |
| BMI | 0.0573 | 0.00800 | <. 0001 | 1.05899 | 1.04251 | 1.07573 |

example 2--bare bones

Association of Predicted Probabilities and Observed Responses

| measure | value | measure | value |
| :--- | :---: | :--- | :--- |
|  |  |  |  |
| Percent Concordant | 53.2 | Somers' D | 0.139 |
| Percent Discordant | 39.3 | Gamma | 0.150 |
| Percent Tied | 7.6 | Tau-a | 0.008 |
| Pairs | 21907512 | c | 0.570 |

example 2--bare bones

Analysis of Maximum Likelihood Estimates \& Odds Ratio (spline model with adjuste

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :--- | ---: | :--- | :--- | :--- | :--- | ---: |
|  |  |  |  |  |  |  |
| Intercept | 1.2414 | 1.0421 | 0.2335 | 3.46050 | 0.44885 | 26.6793 |
| AGE2 | -0.2091 | 0.0816 | 0.0104 | 0.81127 | 0.69139 | 0.9519 |


| AGE3 | -0.2545 | 0.1081 | 0.0185 | 0.77534 | 0.62733 | 0.9583 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| AGE4 | 0.5610 | 0.1785 | 0.0017 | 1.75242 | 1.23497 | 2.4867 |
| PERIOD2 | 0.1342 | 0.0801 | 0.0936 | 1.14365 | 0.97758 | 1.3379 |
| PERIOD3 | -0.0748 | 0.0993 | 0.4514 | 0.92797 | 0.76389 | 1.1273 |
| BMI | -0.2376 | 0.0527 | $<.0001$ | 0.78849 | 0.71107 | 0.8743 |
| BMI1 | 1.4023 | 0.3517 | $<.0001$ | 4.06441 | 2.03987 | 8.0983 |
| BMI2 | -2.8876 | 0.8168 | 0.0004 | 0.05571 | 0.01124 | 0.2762 |

example 2--bare bones

Association of Predicted Probabilities and Observed Responses

| measure | value | measure | value |
| :---: | :---: | :---: | :---: |
| Percent Concordant | 56.2 | Somers' D | 0.195 |
| Percent Discordant | 36.8 | Gamma | 0.209 |
| Percent Tied | 7.0 | Tau-a | 0.012 |
| Pairs | 21907512 | c | 0.597 |

example 2--bare bones

CASE and BMI
PROC LOGISTIC
Data set: MERGE0, with 27102 observations
Outcome variable name: CASE, with 834 events and 26268 non-events
Exposure of interest: BMI
Exposure variable name: BMI
Range of exposure in data used: 16.07 to 39.99
Adjusted for:
age2 age3 age4 period2 period3

Reference value is MIN: 16.07000000
Number of knots: 4
You chose to use all 2 spline variables: BMI1 BMI2

Name of graph file: merge0.BMI.PS

Model w/o exposure of interest, -2 Log Likelihood: 7421.1723178
Linear Model, -2 Log Likelihood: 7374. 2227684
Spline Model, -2 Log Likelihood: 7332.4752231

Line Test Name Description P value

1

| Test for <br> curvature <br> (i.e. non- <br> linear | If the P value is small, the |
| :--- | :--- |
| relation) | exposure and the outcome, if any, |
|  | is non-linear. |
|  | SEE LINE 2. |
|  | If the P value is large, the |
|  | exposure and the outcome, if any |
|  | is linear |
|  | SEE LINE 3. |
|  | If the P value is missing, the |
|  | automatic selection procedure did |
|  | not select any spline variables. |
|  | The relationship between the expo- |
|  | sure and the outcome, if any, is |
|  | linear. SEE LINE 3. | <. 0001


| 2 | Test for overall sig- <br> nificance <br> of the curve | If LINE 1 indicated a possible non-linear relation between the exposure and the outcome, use this $P$ value for the relation of the EXPOSURE to the CASE or TIME. <. 0001 |
| :---: | :---: | :---: |
| 3 | Test for <br> linear <br> relation | If LINE 1 indicated a possible linear relation between the exposure and the outcome, use this $P$ value AND rerun your model with the parameter PWHICH=LINEAR, to get the graph corresponding to the model of interest (if you intend to use the graph). |

First, the macro gives the fractions of the range of BMI that are outside the outer knots. Since the form of the relationship between the EXPOSURE and the CASE is constrained outside the knots, it is desirable that the fraction of the graph outside the knots not be too large. Furthermore, since the outermost knots are at 'worst' at the 5th and the 95th percentiles of EXPOSURE, a large fraction implies that a large area of the graph will represent a very small part of the data. There are two main methods to reduce the fraction of the range outside the knots:

1. Use $K N O T=$ to add one or more knots (e.g. give the same set of knots chosen automatically plus one at the appropriate end;
2. Trim the data (using HPCT, LPCT, HICUT, LOWCUT).

Since HEADER1 was not specified, the output begins by listing the CASE and the EXPOSURE. The graph file has the default name.

The graph is


Note that since we did not give a value for $R E F V A L$, it is 'centered' at the minimum value, 16.07.
Since $H L A B E L$ was not specified, the label for the horizontal axis is just the EXPOSURE variable name. Similarly, the $C A S E$ variable name is shown in the label for the vertical axis.

### 3.3 Example 3. 5 knot spline with given knots and many optional parameters

Below is a call to \%LGTPHCURV9 using a logistic model. In addition, the knots are given using the KNOT parameter to maintain uniformity over a set of analyses. The knot values given are 18.6421 .1423 .5231 .0236 .5 picked by the macro in Example 2, plus one to decrease the fraction of the data outside the knots.

```
%lgtphcurv9(data=merge0, model=logistic, refval=22, exposure=BMI, case=case,
    /* cutoff=2 5,*/ pictname=example3b.ps, outplot=ps, klines=T,
    hlabel=%quote(BMI (kg/sq m)), plotdec=T,
    knot=18.64 21.14 23.52 31.02 36.5,
    vlabel=Odds Ratio for Ovulatory Infertility,
    vlabelstyle=h,
    axlabmult=1.2, axvalmult=1.1,
    ordata=ordata, or=odr, or_lower=lower, or_upper=upper, x_value=mean,
    adj= age2 age3 age4 period2 period3, select=1, plot=2,
    graphtit=Ov Inf vs BMI 4 knot spline adj for age and time pd,
    axordv=0 to 5 by .5);
```

Since I wanted to plot the results from an indicator model (using $O R D A T A$ ), I had to have a data set with the necessary variables. In this case, that data set was named ORDATA. It was made by
running the logistic model with the indicators (PROC LOGISTIC, with the / rl option in the model statement. I could also have used the ODS dataset ORS. I also had to determine some 'central point' for each of the categories represented by the indicators. I computed both the mean and the median. Then I made the data set ORDATA. Each observation has the odds ratio, its lower and upper $95 \%$ confidence limits, and the mean and median of the exposure in the group for which this was the indicator. In calling \%LGTPHCURV9, I decided to use the mean as the x_value for plotting.

As before, the macro noted how much of the range of the exposure was outside the outer knot points. It then listed the knots in both the. $\log$ and the .lst files. Then it printed the values of the spline variables when the $E X P O S U R E$ was set equal to the $R E F V A L$. Finally, it printed the three models (adjusters (covariates) only, adjusters (covariates) plus linear EXPOSURE, adjusters (covariates) plus linear and spline EXPOSURE

The output in the .lst file looks as follows:


```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50
Percent of range of BMI below first knot is 11
Percent of range of BMI above last knot is 15 .
```

```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50
    Knots for BMI:
    18.64 21.14 23.52 31.02 36.5
```

```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50
```

values of spline variables when BMI is 22

| Obs | BMI | BMI1 | BMI2 | BMI3 |
| ---: | ---: | ---: | ---: | ---: |
| 27604 | 22 | 0.11892 | .001994033 | 0 |

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Intercept | -4.7669 | 0.1943 | $<.0001$ | 0.00851 | 0.00581 | 0.01245 |
| BMI | 0.0559 | 0.00795 | <. 0001 | 1.05749 | 1.04113 | 1.07411 |


/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

Analysis of Maximum Likelihood Estimates \& Odds Ratios (linear model with adjust

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Intercept | -4.6925 | 0.1989 | $<.0001$ | 0.00916 | 0.00621 | 0.01353 |
| AGE2 | -0.2243 | 0.0814 | 0.0059 | 0.79904 | 0.68118 | 0.93729 |
| AGE3 | -0.2798 | 0.1078 | 0.0094 | 0.75592 | 0.61198 | 0.93372 |
| AGE4 | 0.5224 | 0.1779 | 0.0033 | 1.68612 | 1.18987 | 2.38934 |
| PERIOD2 | 0.1280 | 0.0799 | 0.1094 | 1.13654 | 0.97171 | 1.32933 |
| PERIOD3 | -0.0780 | 0.0991 | 0.4311 | 0.92496 | 0.76170 | 1.12322 |
| BMI | 0.0573 | 0.00800 | <. 0001 | 1.05899 | 1.04251 | 1.07573 |

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

Association of Predicted Probabilities and Observed Responses

| measure | value | measure | value |
| :--- | :---: | :--- | :--- |
|  |  |  |  |
| Percent Concordant | 53.2 | Somers' D | 0.139 |
| Percent Discordant | 39.3 | Gamma | 0.150 |
| Percent Tied | 7.6 | Tau-a | 0.008 |
| Pairs | 21907512 | c | 0.570 |

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

Analysis of Maximum Likelihood Estimates \& Odds Ratio (spline model with adjuste

| VARIABLE | ESTIMATE | STDERR | PROBCHISQ | ODDSRATIO | LOWERCL | UPPERCL |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |
| Intercept | 0.8925 | 1.0953 | 0.4152 | 2.4412 | 0.28529 | 20.890 |
| AGE2 | -0.2090 | 0.0816 | 0.0104 | 0.8114 | 0.69147 | 0.952 |
| AGE3 | -0.2537 | 0.1081 | 0.0189 | 0.7759 | 0.62779 | 0.959 |
| AGE4 | 0.5603 | 0.1786 | 0.0017 | 1.7513 | 1.23415 | 2.485 |
| PERIOD2 | 0.1334 | 0.0801 | 0.0956 | 1.1427 | 0.97679 | 1.337 |
| PERIOD3 | -0.0744 | 0.0993 | 0.4536 | 0.9283 | 0.76417 | 1.128 |
| BMI | -0.2191 | 0.0556 | $<.0001$ | 0.8032 | 0.72024 | 0.896 |
| BMI1 | 2.4029 | 0.8730 | 0.0059 | 11.0557 | 1.99744 | 61.192 |
| BMI2 | -4.4886 | 2.2016 | 0.0415 | 0.0112 | 0.00015 | 0.841 |
| BMI3 | 1.8342 | 1.5581 | 0.2391 | 6.2601 | 0.29530 | 132.708 |
|  |  |  |  |  |  |  |
| ==================================================================================== |  |  |  |  |  |  |

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

Association of Predicted Probabilities and Observed Responses

| measure | value | measure | value |
| :--- | :---: | :--- | :--- |
|  |  |  |  |
| Percent Concordant | 56.2 | Somers' D | 0.194 |
| Percent Discordant | 36.8 | Gamma | 0.209 |
| Percent Tied | 7.0 | Tau-a | 0.012 |
| Pairs | 21907512 | c | 0.597 |

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:50

Association of Predicted Probabilities and Observed Responses
Ov Inf vs BMI 4 knot spline adj for age and time pd PROC LOGISTIC
Data set: MERGEO, with 27102 observations
Outcome variable name: CASE, with 834 events and 26268 non-events
Exposure of interest: BMI (kg/sq m)
Exposure variable name: BMI
Range of exposure in data used: 16.07 to 39.99
Adjusted for:
age2 age3 age4 period2 period3
Reference value is USER VALUE: 22
Number of knots: 5
You chose to use all 3 spline variables: BMI1 BMI2 BMI3

Name of graph file: example3.ps
Model w/o exposure of interest, -2 Log Likelihood: 7448.592084
Linear Model, -2 Log Likelihood: 7374. 2227684
Spline Model, -2 Log Likelihood: 7331.2779011


1 Test for If the $P$ value is small, the curvature relationship between the
(i.e. non- exposure and the outcome, if any, linear is non-linear. relation) SEE LINE 2.

If the $P$ value is large, the
relationship between the
exposure and the outcome, if any
is linear
SEE LINE 3.
If the $P$ value is missing, the automatic selection procedure did not select any spline variables. The relationship between the exposure and the outcome, if any, is
linear. SEE LINE $3 . \quad$ <. 0001

| 2 | Test for overall significance of the curve | If LINE 1 indicated a possible non-linear relation between the exposure and the outcome, use this $P$ value for the relation of the EXPOSURE to the CASE or TIME. <. 0001 |
| :---: | :---: | :---: |
| 3 | Test for <br> linear <br> relation | ```If LINE 1 indicated a possible linear relation between the exposure and the outcome, use this P value AND rerun your model with the parameter PWHICH=LINEAR, to get the graph corresponding to the model of interest (if you intend to use the graph). <.0001``` |

Three logistic regression models were fit and abbreviated output was printed:

1. The ordinary logistic regression model without the exposure of interest;
2. The ordinary logistic regression model with the exposure of interest entered as a single linear term;
3. The NK-knot spline logistic regression model (with the
```
exposure of interest expressed as EXPOSURE EXPOSURE1 EXPOSURE2 EXPOSURE3
```

--the number of spline variables being 2 less than the number of knots).

Finally, the macro printed out a summary of the whole procedure. It told us the SAS procedure used, the name of the data set used and the number of observations in the data set, the name of the exposure, the name of the outcome variable, the header for the graph, the reference value, the range of the exposure in the data, the list of adjusting variables (covariates), the number of knots, which spline variables were used, and finally the $-2 \log$ likelihoods for the 3 models and the results of the corresponding likelihood ratio tests. In this case, all p values are highly significant.

The test for the overall significance of the curve (Line 2) gives the p-value for the comparison of the spline model with the model having only the adjusters (covariates) (model without the exposure of interest). The test for linear association (Line 3) compares the linear model with the model having only the covariates. The test for non-linearity (Line 1) compares the spline model to the linear model. If the p-value is large (e.g. over . 05 ), you should probably graph the linear relation (i.e. use $P W H I C H=$ LINEAR), though there is some room for judgment here.
The graph is


Note that the graph has a title (HEADER1), that the axes have nice labels (HLABEL and VLA$B E L)$, that the deciles of the data $(0,10, \ldots 100$ percentile levels) are graphed on the $\mathrm{OR}=1$ reference line, that the knot lines are shown, that a smooth histogram is plotted, and that the odds ratios from a model with indicators for BMI levels are also graphed. The footer at the bottom lists the adjusting variables. After running the macro with the default values for the $A X L A B$ $M U L T$ and $A X V A L M U L T$, I decided to make the type a little bigger using $A X L A B M U L T=1.2$ and $A X V A L M U L T=1.1$.

NOTE: In order for the odds ratios and $95 \%$ confidence intervals from the indicator model to coincide (roughly) with the confidence intervals for the spline curve, the spline curve must be centered near the "center" (mean or median) of the reference group in the indicator model. The
bars from the indicator model are located at the horizontal values given by the x_value of their categories. In our example, ORDATA contains variables named MEAN and MEDIAN. If I had used the variable named MEDIAN, the bars would have been in slightly different locations.

NOTE: Since we used the CUTOFF option, both the spline curve and its confidence interval have been truncated at 5 .

IMPORTANT: If you are showing the confidence band as a cloud ( $C I=1$ ) and the curve for the upper confidence limit goes above the upper end of the vertical axis, you must use CUTOFF=2 upper limit. If you do not, the cloud will end abruptly when the upper confidence limit reaches the upper limit. (See Example 4 and Frequently Asked Questions).

### 3.4 Example 4. 3 Knot spline

The macro call is

```
%lgtphcurv9(data=merge0, refval=22, exposure=BMI, case=case,
    pictname=example4.ps, ci=1,
    axordv=0 to 5 by 1,
    hlabel=%quote(BMI (kg/sq m)), nk=3,
    vlabel=Odds Ratio for Ovulatory Infertility,
    adj= age2 age3 age4 period2 period3,
    graphtit=Ov Inf vs BMI 3 knot spline adj for age and time pd,
    adjdat=adjref, modprint=f);
```

The output is
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:52
example 4--3 knot spline
Percent of range of BMI below the first knot is 11 .
Percent of range of BMI above the last knot is 38 .
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:52
example 4--3 knot spline
Knots for BMI:
18.6422 .2431 .02
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:52
example 4--3 knot spline
values of spline variables when BMI is 22

Obs BMI BMI1
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:52 example 4--3 knot spline

```
Ov Inf vs BMI 3 knot spline adj for age and time pd
PROC LOGISTIC
Data set: MERGEO, with 27102 observations
Outcome variable name: CASE, with }834\mathrm{ events and 26268 non-events
Exposure of interest: BMI (kg/sq m)
Exposure variable name: BMI
Range of exposure in data used: 16.07 to 39.99
Adjusted for:
age2 age3 age4 period2 period3
```

Reference value is USER VALUE: 22
Number of knots: 3
You chose to use all 1 spline variables: BMI1
Name of graph file: example4.ps
Model w/o exposure of interest, -2 Log Likelihood: 7448.592084
Linear Model, -2 Log Likelihood: 7374. 2227684
Spline Model, -2 Log Likelihood: 7342.7141655
Line Test Name Description P value
1 Test for If the $P$ value is small, the
curvature relationship between the
(i.e. non- exposure and the outcome, if any,
linear is non-linear.
relation) SEE LINE 2.
If the $P$ value is large, the
relationship between the
exposure and the outcome, if any
is linear
SEE LINE 3.
If the $P$ value is missing, the
automatic selection procedure did
not select any spline variables.
The relationship between the expo-
sure and the outcome, if any, is
linear. SEE LINE $3 . \quad<.0001$

```
2 Test for If LINE 1 indicated a possible
    overall sig- non-linear relation between the
    nificance exposure and the outcome,
    of the curve use this P value for the relation of
    the EXPOSURE to the CASE or TIME. <.0001
3 Test for If LINE 1 indicated a possible
    linear linear relation between the
    relation exposure and the outcome,
    use this P value AND rerun your
    model with the parameter
    PWHICH=LINEAR, to get the graph
    corresponding to the model of
    interest (if you intend to use
    the graph). <.0001
```

The graph is


The graph with 3 knots shows less excess risk at lower values of BMI.
Note that the confidence cloud ends abruptly before the end of the curve. This occurred because the upper confidence limit hit the upper limit of the vertical axes, and I did not use CUTOFF in the macro call..

### 3.5 Example 5. select=3 (automatic stepwise selection)

This is similar to Examples 3 and 4, but this time we use automatic stepwise selection (SELECT=3) to choose from 17 knots. Now that we are experienced in reading the macro output, we use TESTREP=SHORT.

The macro call is

```
title2 'example 5--automatic selection from 17 knot spline';
%lgtphcurv9(data=merge0, model=logistic, refval=22, exposure=BMI, case=case,
    pictname=example5.ps, klines=F, displayx=F, nk=17, select=3,
    hlabel=%quote(BMI (kg/sq m)),
    vlabel=Odds Ratio for Ovulatory Infertility,
    ordata=ordata, or=odr, or_lower=lower, or_upper=upper, x_value=mean,
    adj= age2 age3 age4 period2 period3, plot=2,
    graphtit=Ov Inf vs BMI adj for age and time pd,
    footer=Adjusted for age and time period,
    modprint=f, testrep=short, adjdat=adjref);
```

The partial output is
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53 example 5--automatic selection from 17 knot spline Percent of range of BMI below the first knot is 8 . Percent of range of BMI above the last knot is 23 .

```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline
    Knots for BMI:
    18.02 19.11 19.69 20.12 20.53 20.98 21.31 21.79
    22.24 22.67 23.24 23.91 24.66 25.69 26.95 29.23
    34.39
```

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline
values of spline variables when BMI is 22

| Obs BMI | BMI1 | BMI2 | BMI3 | BMI4 | BMI5 | BMI6 | BMI7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 27604 | 22 | 0.23526 | 0.090073 | 0.045998 | 0.024796 | 0.011854 | .003960073 | .001225886 |
| Obs | BMI8 | BMI9 | BMI10 | BMI11 | BMI12 | BMI13 | BMI14 | BMI15 |
| 27604 | .000034559 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

```
Step 0 : variable BMI1 added
```


/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline

Step 1 : no variable dropped

```
========================================================================================
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline
Step 2 : variable BMI2 added
=======================================================================================
```

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline
Step 3 : no variable added

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline
stepwise procedure cannot add or delete more variables.
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:53
example 5--automatic selection from 17 knot spline

Ov Inf vs BMI adj for age and time pd PROC LOGISTIC
Data set: MERGE0, with 27102 observations
Outcome variable name: CASE, with 834 events and 26268 non-events
Exposure of interest: BMI (kg/sq m)
Exposure variable name: BMI
Range of exposure in data used: 16.07 to 39.99

```
Adjusted for:
    age2 age3 age4 period2 period3
```

Reference value is USER VALUE: 22
Number of knots: 17
You chose to select spline variables automatically, with sls=. 05 and sle=. 05
The following spline variables were selected:
BMI1 BMI2
Name of graph file: example5.ps
Model w/o exposure of interest, -2 Log Likelihood: 7448.592084
Linear Model, -2 Log Likelihood: 7374.2227684
Spline Model, -2 Log Likelihood: 7332.0838498
Line Test Name P value
1 Test for curvature (i.e. non-linear relation) <. 0001
2 Test for overall significance of curve <.0001
3 Test for linear relation <.0001

The graph is


So using the stepwise selection based on the default selection criteria, there are 2 spline variables selected and they are the first and second.

NOTE: The meanings/values of "BMI1" and "BMI2" differ, depending on the number of knots
used and their placement. When $N K=3$ (Example 4), the value of BMI1 when BMI=22 was .24750 . But with the 17 knots, it is .23526 , while with 5 knots (Example 3) it was .11892 .
MORAL: The spline variables are just a way to make pretty curves. Neither they nor their coefficients in the model should be interpreted directly.

The SHORT report on the likelihood ratio tests gives only the p-values.

### 3.6 Example 6. select $=2$ with usersplv

Based on example 5, there are 2 spline variables selected into the model, so if you would like to modify the graph (e.g. fix up the axes or their labels), you don't need to re-run the stepwise selection, which may take a lot of time. Instead, just give the spline variables you want to use. You still need to set $N K$ to 17 to calculate correctly the spline variable values (The reason you still need to set $N K=17$ is that the computations of the spline functions may rely on more knots than those related to the selected spline variables, so if some of those knots are omitted, the spline functions with the same names as those selected will not be the same as those selected originally. See the NOTE above, as well as Section 4, Computational Methods).

The macro call is

```
title2 'example 6--17 knot spline, but use the spline variables selected in example 5';
%lgtphcurv9(data=merge0, model=logistic, refval=22, exposure=BMI, case=case,
        pictname=example6.ps, klines=F, displayx=F, nk=17,
    select=2, usersplv=BMI1 BMI2,
    hlabel=%quote(BMI (kg/sq m)),
    vlabel=Odds Ratio for Ovulatory Infertility,
    ordata=ordata, or=odr, or_lower=lower, or_upper=upper, x_value=mean,
    adj= age2 age3 age4 period2 period3, plot=2,
    graphtit=Ov Inf vs BMI 3 selected from 17 knot spline,
    footer=NONE,
    modprint=f, testrep=short, adjdat=adjref)
```

The output is almost the same as Example 5 except it will point out that you chose to use these spline variables instead of saying that you chose to select spline variables automatically.

```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:55
example 6--17 knot spline, but use the spline variables selected in example 5
Percent of range of BMI below the first knot is 8 .
Percent of range of BMI above the last knot is 23.
```

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:55
example 6--17 knot spline, but use the spline variables selected in example 5
Knots for BMI:
$18.0219 .11 \quad 19.6920 .12 \quad 20.53 \quad 20.98 \quad 21.31 \quad 21.79$
$22.2422 .6723 .2423 .9124 .6625 .6926 .95 \quad 29.23$
34.39


```
/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:55
example 6--17 knot spline, but use the spline variables selected in example 5
values of spline variables when BMI is 22
\begin{tabular}{crcccccccr} 
Obs & BMI & BMI1 & BMI2 & BMI3 & BMI4 & BMI5 & BMI6 & BMI7 \\
27604 & 22 & 0.23526 & 0.090073 & 0.045998 & 0.024796 & 0.011854 & .003960073 & .001225886 \\
Obs & BMI8 & BMI9 & BMI10 & BMI11 & BMI12 & BMI13 & BMI14 & BMI15 \\
27604 & & .000034559 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{tabular}
```

/udd/stleh/doctn/examples.lgtphcurv Program example1-6 06JUL2010 13:55 example 6--17 knot spline, but use the spline variables selected in example 5

```
Ov Inf vs BMI 3 selected from 17 knot spline
PROC LOGISTIC
Data set: MERGEO, with 27102 observations
Outcome variable name: CASE, with }834\mathrm{ events and 26268 non-events
Exposure of interest: BMI (kg/sq m)
Exposure variable name: BMI
Range of exposure in data used: 16.07 to 39.99
Adjusted for:
    age2 age3 age4 period2 period3
Reference value is USER VALUE: 22
Number of knots: 17
You chose to use these spline variables: BMI1 BMI2
Name of graph file: example6.ps
Model w/o exposure of interest, -2 Log Likelihood: 7448.592084
    Linear Model, -2 Log Likelihood: 7374.2227684
    Spline Model, -2 Log Likelihood: 7332.0838498
Line Test Name P value
1 Test for curvature (i.e. non-linear relation) <.0001
2 Test for overall significance of curve <.0001
3 Test for linear relation <.0001
```

The graph is exactly the same as Example 5.

### 3.7 Example 7. plotinc=T; use PRINTPOINTS

This is a pooled logistic example from NHS. The exposure is AGE and the binary outcome is lung cancer. The covariates are cigarettes/day, duration of smoking, age at the start of smoking and the follow-up period.

```
title2 'Example 7--plotting incidence rate';
%lgtphcurv9(data=nhscurr, pictname=example7.ps, plotinc=t,
exposure=age, case=lung19,
header1=%quote(Lung Cancer in NHS, Current Smokers),
footer=%quote(controlling for cigs/d, age began smoking, f-u cycle),
nk=4, klines=f,
testrep=short,
adj=&cig_ &agestr_ &period_, adjdat=adjcurr,
axordh=40 to 80 by 5, refval=40,
axordi=0 to 2000 by 200,
hlabel=Age,
horigin=2,
vlabelstyle=H,
printpoints=40 50 60 70,
vlabeli=Lung Cancer Incidence per }100000\mathrm{ person- years);
```

The final results are

```
/udd/stleh/doctn/lgtphcurv Program example7 17JAN2011 20:22 stleh
Example 7--plotting incidence rate
Lung Cancer in NHS, Current Smokers
PROC LOGISTIC
Data set: NHSCURR, with 101738 observations
Outcome variable name: LUNG19, with }509\mathrm{ events and }101229\mathrm{ non-events
Exposure of interest: Age
Exposure variable name: AGE
Range of exposure in data used: 40 to 78.916666508
Adjusted for:
cig1 cig3 cig4 agestr1 agestr3
period1 period2 period3 period5 period6
period7
Reference value is USER VALUE: 40
Number of knots: 4
You chose to use all 2 spline variables: AGE1 AGE2
Name of graph file: example7.ps
```

Model w/o exposure of interest, -2 Log Likelihood: 6245.3714931
Linear Model, -2 Log Likelihood: 5951.4649953
Spline Model, -2 Log Likelihood: 5936.4018654

Line Test Name P value

1 Test for curvature (i.e. non-linear relation) 0.0005
2 Test for overall significance of curve <.0001
3 Test for linear relation <.0001

| /udd/stleh/doctn/lgtphcurv <br> values for points requested |  |  | Program example7 17JAN2011 20:22 by user as PRINTPOINTS |  |  |  | stleh |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| AGE | PROB | LOWERPRB | UPPERPRB | AGE | INC | LOWERINC | UPPERINC |
| 40 | 0.000154 | 0.000036 | 0.000650 | 40 | 7.679 | 1.812 | 32.52 |
| 50 | 0.001189 | 0.000806 | 0.001755 | 50 | 59.474 | 40.307 | 87.74 |
| 60 | 0.006449 | 0.004924 | 0.008442 | 60 | 322.437 | 246.185 | 422.11 |
| 70 | 0.015978 | 0.011943 | 0.021347 | 70 | 798.904 | 597.156 | 1067.34 |

Note that after the report on the tests for nonlinearity and overall significance, the macro printed the incidence (since we set PLOTINC $=\mathrm{T}$ ) and confidence intervals for the ages requested in PRINTPOINTS.

The graph is


### 3.8 Example 8. A variable without curvature

In the following 3 we revert to the ovulatory infertility study, but the exposure is hours of vigorous exercise per week, from a subset of the data set used in Examples 1-6. The macro reads the data directly frrom a permanent dataset (in libname ellen). The study is restricted to nulliparous nonsmokers using the WHERE and EXTRAV parameters.

The macro call is

```
title2 'example 8';
%lgtphcurv9( data=ellen.merge, exposure=VH, case=case, pictname=example8.ps,
    hlabel=Hours of Vigorous Exercise,
    vlabel=Odds Ratio for Ovulatory Infertility,
    klines=F,
    adj= age2 age3 age4 period2 period3,
    graphtit=Ov Inf vs Vig Ex 4 knot spline adj for age and time pd,
    where=par0 eq 1 and nvsmk eq 1, extrav=par0 nvsmk,
    testrep=short, modprint=f,
    axvalmult=1.1, axlabmult=1.5,
    footer=nulliparous non-smokers, footmult=1.5)
```

The partial output is

```
/udd/stleh/doctn/lgtphcurv Program example8-10 17JAN2011 20:29 stleh
example 8
```

Percent of range of VH below the first knot is 0 .
Percent of range of VH above the last knot is 60 .

| ```/udd/stleh/doctn/lgtphcurv example 8 Knots for VH: 0 0.67 2.5 8.37``` | Program example8-10 | 17 JAN2011 | 20:29 | stleh |
| :---: | :---: | :---: | :---: | :---: |
| /udd/stleh/doctn/lgtphcurv example 8 | Program example8-10 | 17 JAN2011 | 20:29 | stleh |

values of spline variables when VH is 0.00000000

| Obs | VH | VH1 | VH2 |
| :---: | :---: | :---: | :---: |
| 5640 | 0 | 0 | 0 |

/udd/stleh/doctn/lgtphcurv Program example8-10 17JAN2011 20:29 stleh
example 8

Ov Inf vs Vig Ex 4 knot spline adj for age and time pd
PROC LOGISTIC
Data set: ELLEN.MERGE, with 5639 observations
Outcome variable name: CASE, with 385 events and 5254 non-events
Exposure of interest: Hours of Vigorous Exercise
Exposure variable name: VH
Range of exposure in data used: 0 to 21
Adjusted for:
age2 age3 age4 period2 period3

Reference value is MIN: 0.00000000
Number of knots: 4
You chose to use all 2 spline variables: VH1 VH2

Name of graph file: example8.ps

Model w/o exposure of interest, -2 Log Likelihood: 2801.1766207
Linear Model, -2 Log Likelihood: 2785.5279575
Spline Model, -2 Log Likelihood: 2782.3982229

Line Test Name
P value

```
1 Test for curvature (i.e. non-linear relation) 0.2091
2 Test for overall significance of curve 0.0003
3 Test for linear relation 0.0001
```

Since the test for non-linearity has p-value .21 , we will use pwhich=linear in the next graph. This time, the macro used all the spline variables, producing the curvature seen below. We will also switch to $N K=3$, because once you have decided to plot the linear graph, the number of knots is irrelevant (so you might as well use a small number).

The graph is


Note: at the beginning of the macro output, the output notes that $60 \%$ of the range of VH was above the last knot. You can see from the graph that the bulk of the distribution is below 10. We will take care of this problem in Example 10.

### 3.9 Example 9. pwhich=linear, logarithmic vertical axis, horizontal label

The macro call is

```
title2 'example 9';
%lgtphcurv9( data=ellen.merge, model=logistic, pictname=example9.ps,
    hlabel=Hours of Vigorous Exercise, nk=3,
    vlabel=Odds Ratio for Ovula- tory Infer- tility,
    exposure=VH, case=case,
    adj= age2 age3 age4 period2 period3,
```

```
    printcv=T, pwhich=LINEAR,
    displayx=T,
    graphtit=Ov Inf vs Vig Ex linear relation adj for age and time pd,
    adjdat=adjref,
    axordvlog10=T, vlabelstyle=h,
klines=F,
where=par0 eq 1 and nvsmk eq 1, extrav=par0 nvsmk,
testrep=short, modprint=f,
footer=nulliparous non-smokers)
```

Note that the label for the vertical axis $(A X L A B V)$ has hyphenated words with spaces after the hyphens. The macro will put each "word" (i.e. string separated by spaces) on a separate line. It is not desirable for the axis label to take up too much of the space alloted to the graph.

The partial output is

```
example 9
Percent of range of VH below the first knot is 0 .
Percent of range of VH above the last knot is 60.
```

example 9
Knots for VH:
01.258 .37
example 9
values of spline variables when VH is 0.00000000
Obs VH VH1
$5640 \quad 0 \quad 0$
example 9
Ov Inf vs Vig Ex linear relation adj for age and time pd
PROC LOGISTIC
Data set: ELLEN.MERGE, with 5639 observations
Outcome variable name: CASE, with 385 events and 5254 non-events
Exposure of interest: Hours of Vigorous Exercise

```
Exposure variable name: VH
Range of exposure in data used: 0 to 21
Adjusted for:
    age2 age3 age4 period2 period3
Reference value is MIN: 0.00000000
Number of knots: 3
You chose to use all 1 spline variables: VH1
Name of graph file: example9.ps
Model w/o exposure of interest, -2 Log Likelihood: 2801.1766207
                                    Linear Model, -2 Log Likelihood: 2785.5279575
                                    Spline Model, -2 Log Likelihood: 2783.0527101
Line Test Name P value
1 Test for curvature (i.e. non-linear relation) 0.1157
2 Test for overall significance of curve 0.0001
3 Test for linear relation 0.0001
```

example 9

The variance-covariance matrix among all spline variables is:

VH

VH 0.0005

Note that the p value for curvature is different from that in Example 8, because we changed the number of knots.

The graph is


### 3.10 Example 10. Restricting the range of the exposure

There was some concern that the downward direction of the graph was being overly influenced by the (relatively rare) very high values for the exposure. We therefore decided to restrict the data to VH le 10. In general, it is undesirable for a large part of the graph to be generated by very small fraction of the data. In addition, we are supplying a large number of knot values and using automatic selection.

The macro call is

```
title3 'example 10';
%lgtphcurv9( data=ellen.merge, model=LOGISTIC, pictname=example10.ps,
    hlabel=Hours of Vigorous Exercise, select=3, hicut=10,
    knot=0 .3 .5 .7 .9 1.1 1.3 1.5 1.7 1.9 2.1 2.3 2.5 3 3.5
    44.5 5 5.5 6 7 8 9,
    vlabel=Odds Ratio for Ovulatory Infertility,
    exposure=VH, case=case,
    adj=age2 age3 age4 period2 period3,
    n_grid=500, displayx=T,
    e=T, graphtit=Ov Inf vs Vig Ex--automatic selection ,
    plot=2, outplot=PS,
    klines=F, axordv=0 to 1.1 by .1, modprint=F,
    where=par0 eq 1 and nvsmk eq 1, extrav=par0 nvsmk,
    testrep=short,
    footer=nulliparous non-smokers, footmult=1.5);
```

The partial output is

```
example 10
Percent of range of VH below first knot is 0 .
Percent of range of VH above last knot is 10.
example 10
    Knots for VH:
    0.3 . 5 .7 . . 1.1.1 1.3 1.5
    1.7 1.9 2.1 2.3 2.5 3 3.54
    4.555.5678 9
```

example 10
values of spline variables when VH is 0.00000000

example 10
Step 0 : no variable added
example 10
stepwise procedure cannot add or delete more variables.

NOTE: No spline variables are selected by the current criteria.
You can either change the paramter values for sls, sle or nk, or bear in mind the only valid test is the linear test. The graph output will be the linear graph.

```
example 10
    Ov Inf vs Vig Ex--automatic selection
    PROC LOGISTIC
    Data set: ELLEN.MERGE, with }5498\mathrm{ observations
    Outcome variable name: CASE, with }380\mathrm{ events and }5118\mathrm{ non-events
    Exposure of interest: Hours of Vigorous Exercise
    Exposure variable name: VH
    Range of exposure in data used: 0 to 10
    Adjusted for:
        age2 age3 age4 period2 period3
```

    Reference value is MIN: 0.00000000
    Number of knots: 23
    You chose to select spline variables automatically, with sls=. 05 and sle=. 05
    No spline variable is selected by the current criteria
    Name of graph file: example10.ps
    Model w/o exposure of interest, -2 Log Likelihood: 2756.3413559
                            Linear Model, -2 Log Likelihood: 2744.3169145
    There is no spline model available (no spline var.)
    Line Test Name P value
    1 Test for curvature (i.e. non-linear relation).
    2 Test for overall significance of curve .
    3 Test for linear relation 0.0005
    Note that the number of observations in the output from using $H I C U T=10$ is lower than the number in the original set of nulliparous nonsmokers. You can also use $H P C T$ or $L P C T$ to delete observations with $E X P O S U R E$ beyond speficied upper or lower percentiles.

The graph is


### 3.11 Example 11. Conditional logistic regression (MODEL=condlog)

This option normally is used if you have a matched case-control study, that is, if you would like to use a conditional logistic model for your data. The code below calls \%LGTPHCURV9 to do a conditional logistic regression in a matched case-control study of LDL cholesterol and CHD, controlling for age, hypertension, BMI, HDL cholesterol, and aspirin use.

The macro call is

```
title2 'example 11a--conditional logistic regression';
%lgtphcurv9(data=lipids, model=condlog, strata=matchid, time=censor,
case=cc, exposure=ldl_c,
header1=LDL cholesterol and CHD, graphtit=NONE,
adj=hdlg2 hdlg3 hdlg4 hdlg5 agegp4 agegp6 hbp90f asp90 bmi2530 bmi30hi ,
pictname=condlogex.ps,
pwhich=spline, axordh=50 to 300 by 50, axordv=0 to 6 by 1, klines=T,
refval=100, vlabel=Relative Risk of CHD, hlabel=LDL Cholesterol,
footer=%quote(Adjusted for HDL chol, age, hypertension, aspirin use, and BMI),
testrep=short, modprint=f,
plot=2);
```

Note that in this macro call, we specified a FOOTER listing the conceptual variables.
The output is
/udd/stleh/doctn/lgtphcurv Program example11ab 17 JAN2011 $20: 37 \quad$ stleh
example 11a--conditional logistic regression
Percent of range of LDL_C below the first knot is 13.
Percent of range of LDL_C above the last knot is 42 .

/udd/stleh/doctn/lgtphcurv Program example11ab 17JAN2011 20:37 stleh
example 11a--conditional logistic regression
Knots for LDL_C:
77.3121 .2150197 .8
/udd/stleh/doctn/lgtphcurv Program example11ab 17JAN2011 20:37 stleh
example 11a--conditional logistic regression
values of spline variables when LDL_C is 100

| Obs | LDL_C | LDL_C1 | LDL_C2 |
| :---: | :---: | :---: | :---: |
| 1172 | 100 | 0.80557 | 0 |

/udd/stleh/doctn/lgtphcurv Program example11ab 17JAN2011 20:37 stleh example 11a--conditional logistic regression

LDL cholesterol and CHD
PROC PHREG
Conditioned on matchid
Data set: LIPIDS, with 670 observations
Time variable name: CENSOR
Censoring variable name: CC with 222 events and 448 censored
Exposure of interest: LDL Cholesterol
Exposure variable name: LDL_C
Range of exposure in data used: 43.9 to 307.7
Adjusted for:
hdlg2 hdlg3 hdlg4 hdlg5 agegp4
agegp6 hbp90f asp90 bmi2530 bmi30hi

Reference value is USER VALUE: 100
Number of knots: 4
You chose to use all 2 spline variables: LDL_C1 LDL_C2

Name of graph file: condlogex.ps

Model w/o exposure of interest, -2 Log Likelihood: 398.9986202
Linear Model, -2 Log Likelihood: 390.34610796

```
Line Test Name P value
```

```
1 Test for curvature (i.e. non-linear relation) 0.4499
2 Test for overall significance of curve 0.0166
3 Test for linear relation 0.0033
```

The graph is


Note that, although there seems to be a ceiling effect, the test for curvature is non-significant.
Because of the large fraction of the range of the data above the last knot and given the lack of evidence for curvature, we decided to try a second model with data trimmed at the 1st and 98th percentiles, with a $P W H I C H=$ linear.

The macro call is:

```
options ps=40;
title2 'example 11b--conditional logistic regression, trimmed';
%lgtphcurv9(data=lipids, model=condlog, strata=matchid, time=censor,
case=cc, exposure=ldl_c,
adj=hdlg2 hdlg3 hdlg4 hdlg5 agegp4 agegp6 hbp90f asp90 bmi2530 bmi30hi ,
pictname=example11b.ps,
header1=LDL cholesterol and CHD,
```

```
hpct=98, lpct=1,
pwhich=linear, axordh=50 to 250 by 50, axordv=0 to 6 by 1, klines=T,
testrep=short, modprint=f,
footer=%quote(Adjusted for HDL chol, age, hypertension, aspirin use, and BMI),
refval=100, vlabel=Relative Risk of CHD, hlabel=LDL Cholesterol,
plot=3);
options ps=78;
```

Trimming the data made very little difference to the location of the knots, but the fraction of the data outside the outer knots is greatly reduced.

The output is:
example 11b--conditional logistic regression, trimmed
Percent of range of LDL_C below the first knot is 12 .
Percent of range of LDL_C above the last knot is 17 .

```
example 11b--conditional logistic regression, trimmed
    Knots for LDL_C:
    81 121.1 149.1 189
```


example 11b--conditional logistic regression, trimmed
values of spline variables when LDL_C is 100
Obs LDL_C LDL_C1 LDL_C2
$1154 \quad 100 \quad 0.58805 \quad 0$
example 11b--conditional logistic regression, trimmed
LDL cholesterol and CHD
PROC PHREG
Conditioned on matchid
Data set: LIPIDS, with 652 observations
Time variable name: CENSOR
Censoring variable name: CC with 215 events and 437 censored
Exposure of interest: LDL Cholesterol

```
Exposure variable name: LDL_C
Range of exposure in data used: 63 to 215.3
Adjusted for:
    hdlg2 hdlg3 hdlg4 hdlg5 agegp4
    agegp6 hbp90f asp90 bmi2530 bmi30hi
Reference value is USER VALUE: }10
Number of knots: 4
You chose to use all 2 spline variables: LDL_C1 LDL_C2
Name of graph file: example11b.ps
Model w/o exposure of interest, -2 Log Likelihood: 378.48496646
    Linear Model, -2 Log Likelihood: 369.55368676
    Spline Model, -2 Log Likelihood: 368.56755254
Line Test Name P value
1 Test for curvature (i.e. non-linear relation) 0.6108
2 Test for overall significance of curve 0.0193
3 Test for linear relation 0.0028
```

Line 1 shows that we were justified in using $P W H I C H=$ linear, even on the trimmed data set. The graph is:


### 3.12 Example 12. MODEL=COX

This example uses data from a study of fibroids (uflap) in NHS II. The main exposure is BMI (bmicp). The time variable is sdytime. The covariates are time started antihypertensive medications (tv2da), race/ethnicity (raceth), age at menarche (meng), age at first OC use (foc), age at first birth (afbi), marital status (marryg), time since last birth (tslbf), infertility (fail), irregular menses (irreg).

The macro call using 5 knots automatically placed is

```
%lgtphcurv9(data=fibroid1, time=sdytime, strata=agemo period, model=cox,
exposure=bmicp, where=bmimp eq 0, extrav=bmimp, refval=25,
case=uflap,
hicut=44, lowcut=16, nk=5,
adj=tv2da2 tv2da3 tv2da4 tv2da5 tv2da6 tv2da7 tv2da8 tv2da9
afbi1 afbim
fail1 failm
foc0 foc1 foc3 foc4 focm
irreg1 irreg2 irregm
marryg1
meng1 meng2 meng4 meng5 meng6 meng7 mengm
raceth2 raceth3 raceth4 racethm
tslbf0 tslbf2 tslbf3 tslbfm,
plot=2, testrep=short, modprint=f,
hlabel=%quote(BMI (kg/sq m)), axordh=16 to 44 by 4,
vlabel=Relative Risk of Fibroids, axordv=.5 to 1.5 by .1,
pictname=example12a.ps,
```

```
header1=BMI and Fibroids, graphtit=NONE, footer=NONE);
```

Since the model outputs are long and not very informative, we give partial output here.

| /udd/stleh/doctn/examples.lgtphcurv Program example12 | 06 JUL2010 | 14:34 |
| :---: | :---: | :---: |
| Percent of range of BMICP below the first knot is 11 |  |  |
| Percent of range of BMICP above the last knot is 31 |  |  |

/udd/stleh/doctn/examples.lgtphcurv Program example12 06JUL2010 14:34 st Knots for BMICP: 19.0521 .3123 .426 .5435 .36
/udd/stleh/doctn/examples.lgtphcurv Program example12 06JUL2010 14:34 st
values of spline variables when BMICP is 25

Obs BMICP BMICP1 BMICP2 BMICP3

| 414109 | 25 | 0.79185 | 0.18887 | 0.015398 |
| :--- | :--- | :--- | :--- | :--- |

/udd/stleh/doctn/examples.lgtphcurv Program example12 06JUL2010 14:34 st

```
BMI and Fibroids
PROC PHREG
Conditioned on agemo period
Data set: FIBROID1, with 413607 observations
Time variable name: SDYTIME
Censoring variable name: UFLAP with }7103\mathrm{ events and }406504\mathrm{ censored
Exposure of interest: BMI (kg/sq m)
Exposure variable name: BMICP
Range of exposure in data used: 16 to 43.94
Adjusted for:
    tv2da2 tv2da3 tv2da4 tv2da5 tv2da6
    tv2da7 tv2da8 tv2da9 afbi1 afbim
    fail1 failm foc0 foc1 foc3
    foc4 focm irreg1 irreg2 irregm
    marryg1 meng1 meng2 meng4 meng5
    meng6 meng7 mengm raceth2 raceth3
```

```
raceth4 racethm tslbf0 tslbf2 tslbf3
tslbfm
```

```
Reference value is USER VALUE: }2
Number of knots: 5
You chose to use all 3 spline variables: BMICP1 BMICP2 BMICP3
Name of graph file: example12a.ps
Model w/o exposure of interest, -2 Log Likelihood: 84047.804272
    Linear Model, -2 Log Likelihood: 82877.256564
    Spline Model, -2 Log Likelihood: 82857.157407
```

Line Test Name $\quad P$ value
1 Test for curvature (i.e. non-linear relation) 0.0002
2 Test for overall significance of curve <.0001
3 Test for linear relation <.0001

The graph is


Since the knots leave a large space in the middle, and the last knot point is far from the maximum of the exposure range, we tried giving the macro 5 knots, placed at 19, 24, 30, 35, and 40.

The p-value for non-linearity was .0003 .
The graph is

Finally, we gave the macro 14 knots (18, 19, 20, 21, 22, 23, 24, 25, 26, 28, 30, 33, 36, 40) and used automatic selection.

3 spline variables ( 1,2 , and 6 ), and the p value for non-linearity was .0003 .
The graph is


Note that all the graphs look much the same, regardless of the placement of the knots used.

## 4 Computational Methods

### 4.1 Automatic knot placement, given a desired number of knot points

If you specify a number of knots $(N K)$, the macro will automatically determine the appropriate percentiles of the data and place the knots there. If you request automatic spline variable selection $(S E L E C T=3)$ and have not given $N K$, the macro will set $N K=21$. If you do not give $N K$ or KNOT and do not use automatic spline variable selection, the macro will set $N K=4$. As always, this can be overridden by providing a list of knot locations.

```
NK Knot locations as percentiles of EXPOSURE
-- ----------------------------
3 5 50 95
4 5 35 65 95
5 5 27.5 50 72.5 95
6 5 23 41 59 77 95
7 2.5 18.3333 34.1667 50 65.8333 81.6667 97.5
8 1 15 29 43 57 71 85 99
9 2 14 26 38 50 62 74 86 98
10 2 12.6667 23.3333 34 44.6667 55.3333 66
    76.6667 87.3333 98
17}208814 20 26 32 38 44 50 56 62 68 74 80 86 92 98
21 1444 14 19 24 29 34 39 44 49 54 59 64 69 74 79 84 89 94 99
25 2 6 10 14 18 22 26 30 34 38 42 46 50
    54 58 62 66 70 74 78 82 86 90 94 98
50 1 3 5 7 9 11 13 15 17 19 21 23 25 27
    29 31 33 35 37 3941434547 49 51
    5355 57 59 61 63 65 67 69 71 73 75
    77 79 81 83 85 87 89 91 93 95 97 99
```


### 4.2 Computation of the spline variables:

Let $t_{j}$ be the jth knot point.
Let $k d=\left(t_{n k}-t_{1}\right)^{2 / 3}$, where $k d$ is a normalizing parameter to get the spline variables back into the original units.

For a level of the exposure $\mathrm{x}, x_{j}$, the value of the j th spline variable ( j runs from 1 to NK-2) is given by

$$
\begin{gathered}
x_{j}=\max \left(\left(x-t_{j}\right) / k d, 0\right)^{3} \\
+\left(t_{n k-1}-t_{j}\right) * \max \left(\left(x-t_{n k}\right) / k d, 0\right)^{3} \\
\left.-\left(t_{n k}-t_{j}\right) * \max \left(\left(x-t_{n k-1}\right) / k d, 0\right)^{3}\right) /\left(t_{n k}-t_{n k-1}\right)
\end{gathered}
$$

For $x<t_{j}$ the value of the j th spline variable is 0 (as are the 'higher' spline variables) (because all the 'max' values are 0 , since $x<t_{j}<t_{n k-1}<t_{n k}$. As x gets larger, it has more and more nonzero spline variables.

Note that the value of $x_{j}$ depends on the values of the first, $n k$ th, and $n k$ - 1 st knots. That is why the value of the spline variable depends on the locations of knots other than the $j$ th knot.

### 4.3 Default bandwidth for smoothing:

The default bandwidth is data-specific. Let N be the size of the data set, and STD be the standard deviation of the exposure variable ( X ) in the data set.

$$
\text { bandwidth }=(S T D / 1.349) *(4 / 3 N)^{0.2}
$$

Although the user can set the bandwidth (using $B W M$ ), it is usually fine to let the macro do it automatically. See Frequently Asked Questions below.

### 4.4 Outline of stepwise model selection:

If you request automatic spline variable selection (em SELECT=3) and have not specified $N K$, the macro will set $N K=21$. As always, this can be overridden by providing a list of knot locations.

The default $S L E$ and $S L S$ for automatic selection are .05 , but the user may specify other values.
In the discussion below, all mentions of 'likelihood' should be interpreted to mean 'partial likelihood' when Cox models are used.

Each step starts with a 'base' model. For the first step, the 'base' model includes the linear term and all the adjusters. For subsequent steps, the 'base' model includes the above plus whatever spline variables are in the model by the end of the step.

For a forward step, each of the spline variables not in the base model is added (singly) to the base model and a likelihood is computed. If, for the spline variable giving the biggest likelihood (i.e. the biggest change from the base model), the likelihood ratio test (LRT) gives a p-value meeting the criterion for entry into the model (SLE), that spline variable is added to the model. Otherwise, no variable is added to the model.

For a backward step, each of the spline variables in the base model is deleted (singly) from the base model, and a likelihood is computed. If, for the spline variable giving the biggest likelihood (i.e. the closest to the base model), the LRT gives a p-value greater than the criterion for staying in the model (SLS), that spline variable is dropped from the model. Otherwise, no variable is dropped. If a variable is dropped, the macro uses this new base model and tests the remaining spline variables to see whether they can be dropped.

Forward and backward steps alternate until two (2) steps in a row do not change the model, or until the maximum number of steps is attained (default=10).

## 5 Warnings

It is not currently possible to plot the predicted probability and the OR or IRR on the same graph.

## 6 Frequently Asked Questions

### 6.1 Q: Why is the confidence band so wide?

A: A common reason for this is that parts of the range of the exposure have very few observations. This is most likely to occur at the extremes of the data. It shows up as long flat tails in the smoothed histogram. You can also look at the knot positions. For 3 and 4 knot splines, the outer knots are at the 5 th and 95 th percentile points. If these are far from the lowest and highest values in the data you are using, you may need to trim the data, either by values of the exposure (HICUT, $L O W C U T$ ) or by percentiles of the exposure distribution $(H P C T, L P C T)$. If you cannot do that, then use the cutoff parameter.

### 6.2 Q: Why are the values on the horizontal axis printing out vertically?

A: You probably asked for too many major tick marks.
$A X O R D H$ should be written so that about 8 to 12 numbers will print out, such as

```
axordh=0 to 100 by 10
```

rather than

```
axordh=0 to 100 by 5
```

This could also happen if you let the macro determine the tick marks and they are not 'round.' In this case, you should see what the graph looks like and determine the horizontal axis ticking yourself.

### 6.3 Q: Why does the confidence "cloud" stop abruptly in the middle of the graph?

A: This happens when the upper limit of the confidence "cloud" goes above the upper limit of the graph. To fix this, use $C U T O F F$.

### 6.4 Q: I want to plot the smoothed histogram, but the SAS .log says that the Sheather-Jones plug-in did not converge

A: Sometimes the Sheather-Jones plug-in does not work. You can try increasing the smoothing parameter $(B W M)$ or using $D I S T M E T H=\mathrm{OS}$.

### 6.5 Q: How do I put more than one spline curve on a graph?

A: At the moment, the macro does not accommodate 'by' variables. To put more than one curve on a single graph, you need to run \%LGTPHCURV9 to get each curve. If the curves are for subsets of a larger dataset, you can do this using the WHERE parameter. Don't forget to use EXTRAV if a variable occurs in the WHERE parameter but nowhere else. In each run of \%LGTPHCURV9, you
set $P L O T=4$ and PLOTDATA to something that will remind you of which group you are dealing with (e.g. smokca.men and smokca.women). Once you have the plotting information, you can plot both in excel, or read them into SAS and use SASGRAPH.

### 6.6 Q: Why are the coefficients of the spline variables so large in absolute value?

A: Because the spline variables are often highly correlated, it is not unusual for the coefficients to alternate between very negative and very positive values.

### 6.7 Q: Why did SAS print a WARNING saying it ignored the ORDER = list on the axis statement?

A: This happens when you use AXORDVLOG10=T (see Invocation and Details above). It is harmless.

### 6.8 Q: I got an error saying the $x$-origin did not leave enough space for the text.

Here is an example of the ERROR message:

```
ERROR: The specified x-origin for the left vertical axis labeled LOWER did not
    leave enough space for the text. You need to specify ORIGIN=( 2.1 INCH
    ). The graph was not produced.
```

A: This can happen when you use $V L A B E L S T Y L E=\mathrm{H}$, if some of the words are too long. Try hyphenating the longest words OR change the HORIGIN as suggested by the ERROR message. This latter will make your actual graphics area smaller to accommodate your axis label.

### 6.9 Q: How do I make ADJDAT?

A: If you are plotting probabilities or incidence rates, you need to have values of the covariates at which to plot them. The choice of covariate values will influence the absolute value of the probabilities or incidence rates, but not the shape of the curve. It is often convenient to use the reference levels of all the sets of indicators (or alternatively, the middle indicator), and the medians or some conventional value for the continuous variables (other than the exposure, which should not have a value in this dataset). One way to do this, especially if you have a lot of sets of indicators is as follows:

```
data adjdat;
array nums ....... ; /* the list of all the adjusters. you can just copy it from the ADJ parar
do over nums; nums=0; end ; /* effectively sets all sets of indicators to their reference
/* special coding for continuous variables */
bmi76=25; /* coding to a conventional cutoff */
run;
```

Below are the steps for importing an encapsulated postscript file into a MS-WORD
document.
\begin\{verbatim\} }

1. E-mail the file to yourself as an attachment, and download to your PC.
2. Open your WORD document.
3. The sequence of keys (at least in Windows XP and its version of WORD) is
insert
picture
from file
<locate file>
convert file (this is a window that WORD gives you)
encapsulated postscript

NOTE: Conversion from encapsulated postscript may not be installed on your computer, but it is available for Windows 95 and beyond. NOTE: When I did the above procedure the picture on my Windows screen was fuzzy. When printed, it was crisp.

If you are really having trouble, consider using one of the other formats (HTML, JPEG, CGM).

## 7 How should I describe this in my Methods section?

The wording below has been approved by Prof. Donna Spiegelman.
We examined the possibly non-linear relation between insert the name of the exposure here and insert the name of the outcome here, such as the $R R$ of -- non-parametrically with restricted cubic splines [REF Durrleman and Simon]. Tests for non-linearity used the likelihood ratio test, comparing the model with only the linear term to the model with the linear and the cubic spline terms.

## 8 Credits

This macro is based on a restricted cubic spline macro originally written by Frank Harrell. Any questions should be addressed to Ruifeng Li via email strui@channing.harvard.edu or via phone 617-432-6321.

## 9 References

Some references are

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Harrell, Frank E, Jr., Lee, Kerry L., Pollock, Barbara G.:
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between predictors and response. JNCI 80: 1198-1202, 1988.

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models with cubic splines. Statistics in Medicine 8: 551-561, 1989.

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A reference for the binned kernel density estimator (smoothed histogram) is

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A reference discussing the presentation of the confidence bands is

Greenland, S., Michels, K.B., Robins, J.M., Poole, C., Willett, W.C.: Presenting statistical uncertaintly in trends and dose-response relations. Am J Epidemiol 149: 1077-1086, 1999.

